## Definitions.

Let T denote some transformation.

Let (m) denote some object (simple or complex).

Let "->" denote the process of transformation.

Let T(m) -> (n) be read "transformation T on object m produces object n".

Let  $T_2T_1$  be read "do transformation 1 first, followed by transformation 2".

## Properties of transformations.

1) A transformation on an object must produce a unique result such that

if 
$$T(m) -> (n)$$
 and  $T(m) -> (p)$ , then  $(n) = (p)$ .

2) Some transformations are not directly perceivable. Such a transformation may only be inferred by the observer when it operates on multiple objects (i.e., a complex object).

If 
$$T(2) \rightarrow (4)$$
, then  $T = "+2" = "x2"$   
But if  $T(2, 3, 19) \rightarrow (4, 5, 21)$ , then  $T = "+2"$ .

3) Transformations may be combined such that

if 
$$T_1(m) \rightarrow (n)$$
 and  $T_2(n) \rightarrow (p)$ , then  $T_2T_1(m) \rightarrow (p)$ .

4) Transformations do not always commute (i.e., the order in which they are done makes a difference).

If 
$$T_1="+a"$$
 and if  $T_2="xb"$ , then  $T_2T_1 \neq T_1T_2$ .

5) There exists an identity transformation, denoted T<sub>0</sub>, which doesn't change the object such that

$$T_0(m) -> (m)$$
.

6) Some transformations are undoable.

If  $T_1(m) \rightarrow (n)$  and  $T_{-1}(n) \rightarrow (m)$ , then both  $T_1$  and  $T_{-1}$  are undoable and each is the "inverse" of the other such that their combination produces the identity where  $T_{-1}T_1=T_0$ .

7) Some transformations are their own inverses such that

If 
$$T(m) \rightarrow (n)$$
, then  $T(n) \rightarrow (m)$ . Therefore,  $TT=T_0$ .

8) Some transformations combine objects. These are called "combining transformations" and are denoted "\*" such that

(m) \* (n) = the combination of (m) and (n). Combining transformations are not undoable and therefore have no inverses.

## Tape studio transformations and their properties.

- 1) Tape dubbing (copying a pre-recorded sound from one tape to another). Properties 1 and 5.
- 2) Tape speed change (changes the pitch and duration of a pre-recorded sound). Propertries 1, 2, 3, 6.
- 3) Tape direction change (makes pre-recorded sounds sound backwards). Properties 1, 2, 3, 6, 7.
- 4) Tape splicing (removal of time-segments of pre-recorded sound or re-ordering of segments). Properties 1, 2, 3, 6.
- 5) Tape mixing (combining two or more tracks of sound into one track). Properties 1, 2, 8.
- 6) Filtering or equalization (changes timbre). Properties 1, 2, 3, 6.
- 7) Digital delay (combines normal sound with delayed sound). Properties 1, 4, 8.
- 8) Frequency modulation effects (two frequencies are multiplied together). Properties 1, 3, 4, 8.